

# Coupling Lorentz Integral Transform and Coupled Cluster Methods: a way towards continuum spectra of not-so-light systems.

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The Lorentz Integral Transform (LIT) method allows to calculate spectra in the continuum, without dealing with the many-body scattering problem. The method consists in reducing the continuum problem to a bound state one, when calculating the spectra, (discrete and/or continuum) of a many-body system. In fact the response  $S(\omega)$  of a system to a perturbative reaction induced by the operator  $\Theta$  can be accessed by first calculating, and then inverting, the integral transform of  $S(\omega)$  with a Lorentzian kernel  $K(\omega, \omega_0, \Gamma) = \Gamma[\pi((\omega - \omega_0)^2 + \Gamma^2)]^{-1}$ . The main point is that the LIT of  $S(\omega)$  can be calculated much more easily than  $S(\omega)$  itself. In fact it turns out that the LIT of  $S(\omega)$  is the norm of the solution  $|\tilde{\psi}\rangle$  of the following bound state-like equation

$$(H - z)|\tilde{\psi}\rangle = \Theta|0\rangle, \quad (1)$$

where  $z = \omega_0 + i\Gamma$ .

The method has been applied successfully on few-body systems for  $A=3$  and  $4$ , using both realistic and chiral effective field theory potentials (including also three-body forces), and to  $A=6$  and  $7$  with semirealistic central potentials. For all these systems the solution of the bound-state-like equation (1), representing the core of the method, has been solved using typical bound-state approaches, like hyperspherical harmonics or no-core-shell-model expansions, as well as the Faddeev-Yakubowski formulation (see Ref.[1] for a review).

In view of extending the range of applicability of the LIT method to larger systems we have formulated Eq. (1) using the Coupled Cluster (CC) technique (see Ref. [2] for a review). Here one has to solve a right Schrödinger-like equation

$$(\bar{H} - z)|\tilde{\psi}_R\rangle = \bar{\Theta}|0_R\rangle, \quad (2)$$

where  $\bar{H}(\bar{\Theta}) = \exp(-T)H(\Theta)\exp(T)$  are the similarity transformed Hamiltonian(excitation operator). The state  $|0_R\rangle$  is the ground-state of the non-hermitian similarity-transformed Hamiltonian and  $|\tilde{\psi}_R\rangle = R|\phi_0\rangle$  where  $|\phi_0\rangle$  is a Slater determinant and the operator  $R$  is a linear expansion in particle-hole excitations. One has also to solve an equivalent left

Schrödinger-like equation for  $\langle \tilde{\psi}_L | = \langle \phi_0 | L$  where  $L$  can be written via an expansion equivalent to that for  $R$ . In the CCSD approximation we truncate  $T$  as well as  $R$  and  $L$  at the  $2p$ - $2h$  excitation level. The LIT of  $S(\omega)$  is given by  $\langle \tilde{\psi}_L | \tilde{\psi}_R \rangle$ . It can be computed efficiently by employing a generalization of the Lanczos algorithm for non-symmetric matrices in the solution of the linear problem in Eq. (2).

Figure 1 represents the calculated LIT ( $\Gamma = 10$  MeV) of  $S(\omega)$  for  $^{16}\text{O}$  and  $\Theta$  equal to the dipole operator. The Hamiltonian contains the chiral effective field theory two-nucleon potential from Ref. [3]. The theoretical result is compared to experimental data by folding the  $S(\omega)$  obtained from photonuclear cross section measurements [4] with a Lorentzian of 10 MeV width. One notices the presence of a peak, which is the *remnant* of the giant dipole resonance (GDR). In spite of the lack of three-nucleon forces the position of the GDR is rather well reproduced. It will be interesting to check if this result is accidental, when three-nucleon forces are included. More informations will be obtained by inverting the transform.

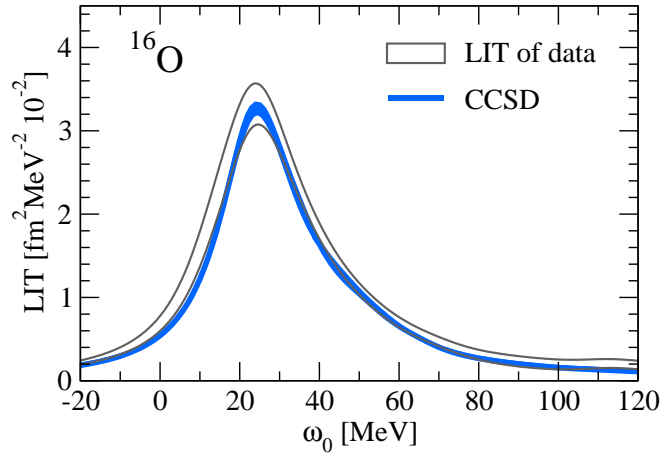


Figure 1: Comparison of the LIT of the dipole response of  $^{16}\text{O}$  calculated within CCSD at  $\Gamma = 10$  MeV and the LIT of the photonuclear data from Ref. [4].

- [1] Efros, V.D., Leidemann, W., Orlandini, G., Barnea, N.: Journal of Phys. G 34, R459 (2007)
- [2] Bartlett, R.J., Musial, M.: Rev. Mod. Phys. 79, 291 (2007)
- [3] Entem D.R., Machleidt, R.: Phys. Rep. 503,1 (2011)
- [4] Ahrens, J., et al.: Nucl. Phys. A 251, 479 (1975)

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